

Anderton Primary School Maths Mastery Calculation Policy

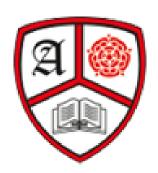


Date reviewed:

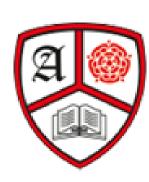
Date for next review:

Signed:

Signed:

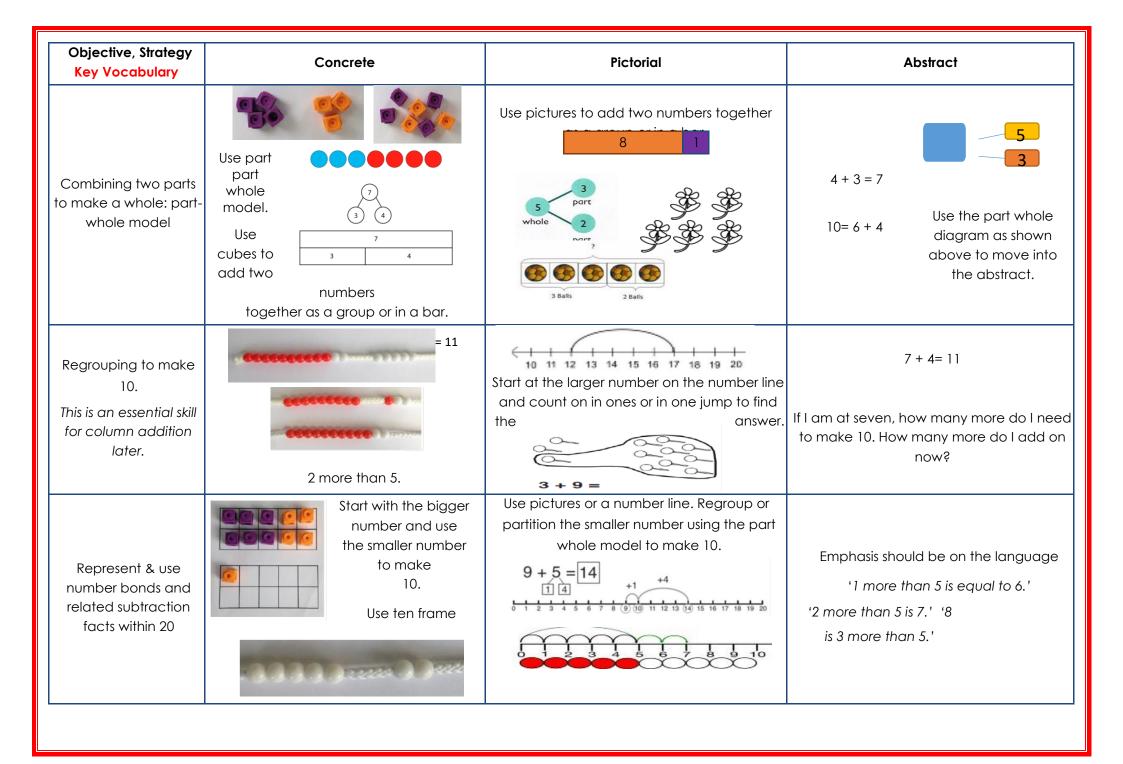


Year 1 Addition



Objective, Strategy Key Vocabulary	Concrete	Pictorial	Abstract
Comparing Objects, groups of objects Length, weight, mass, heavier, lighter, same, equal	People's height, distance, mass. Use of pan balances using Numicon or similar to show equivalence, < > Comparing multiple objects Use of concrete materials eg. Compare bears, jewels, cubes etc to create groups of different sizes to compare		
Using < > and = Fewer, more, less than, more than, equal to, fewer than	Use a multilink staircase in two colours	1<3 2 = 2 3>1	Use variation with missing boxes and missing symbols. 3
Finding one more, finding one less	1 2 3 4 5 6 7 8 9 10	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	One more/less sentences – example one: 1 more than 3 is 1 less than 2 is 1 more than is 1 1 less than is 1

Objective, Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
Adding 1 gives 1 more	First Then Now 3 +1 4	First Then Now	6 + 1 7 6 + 1 = 7
Augmentation— increasing an amount	Use FIRST, THEN, NOW and range of practical situations for showing augmentation. E.g. first there were three chn on carpet then 2 more came. Now there are 5 chn on the carpet.	First Then Now	4 +3 7 4+3=7
Stories of numbers within 10	Children should work with doubled sided counters and ten frame. Start with 7 red, turn one over, tell me the 'story'? Turn one more over. What is the 'story'? Continue. Complete this for stories of all numbers up to 10.	7 + 0 = 7 6 + 1 = 7 5 + 2 = 7 etc Complete for all numbers up to 10	7 + 0 = 7 $6 + 1 = 7$ $5 + 2 = 7$ $4 + 3 = 7$ $3 + 4 = 7$ $2 + 5 = 7$ $1 + 6 = 7$ $0 + 7 = 7$



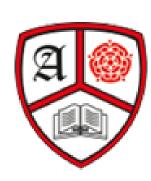
YI facts Bridging/ Adding I and 2 Bonds to 10 Adding 10 compensating Near doubles Doubles Adding 0 2 3 5 9 7 10 8 0 4 6 + 0 0 + 50 + 00 + 10 + 20 + 30 + 40 + 60 + 70 + 80 + 90 + 101 + 01 + 21 + 31 + 51 + 71 + 81+9 1 + 10I + I1 + 41+6 2 2 + 02 + 22 + 32 + 72 + 82 + 92 + 102 + 12 + 42 + 52 + 63 3 + 73 + 03 + 53 + 63 + 83 + 93 + 103 + 13 + 23 + 33 + 44 4 + 04 + 34+4 4 + 54+6 4 + 74 + 84 + 94 + 104 + 14 + 25 5 + 05 + 15 + 25 + 35 + 45 + 55 + 65 + 75 + 85 + 95 + 106 6 + 46 + 56 + 96 + 106 + 06 + 16 + 26 + 36+6 6 + 76 + 87 7 + 37 + 07 + 17 + 27 + 47 + 57 + 77 + 87 + 97 + 107 + 68 8 + 08 + 18 + 28 + 38 + 48 + 58 + 6 8 + 78+8 8 + 98 + 109 9 + 09 + 19 + 29 + 39 + 49 + 59 + 69 + 79 + 89 + 99 + 1010 10 + 010 + 110 + 210 + 310 + 410 + 510+6 10 + 710 + 810 + 910 + 10

Y2

facts



Year 2 Addition



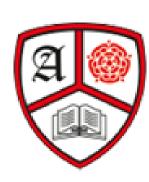
Objective & Strategy & Key Vocabulary	Concrete	Pictorial	Abstract
Adding multiples of ten	50= 30 + 20 Model using dienes and bead strings	tens and tens makes tens Use representations for base ten.	20 + 30 = 50 70 = 50 + 20 40 + \(\pi\) = 60 \(\pi\) + 30 = 50
Use known number facts Part part whole	Children explore ways of making numbers within 20	20	☐ + 1 = 16
Using known facts	Ted Sam	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 + 4 = 7 Leads to 30 + 40 = 70 Leads to 300 + 400 + 700 '3 things and 4 things is always 7 things'
Bar model	3 + 4 = 7	8 3 + 5 = 8	30 14 16 14 + 16 = 30

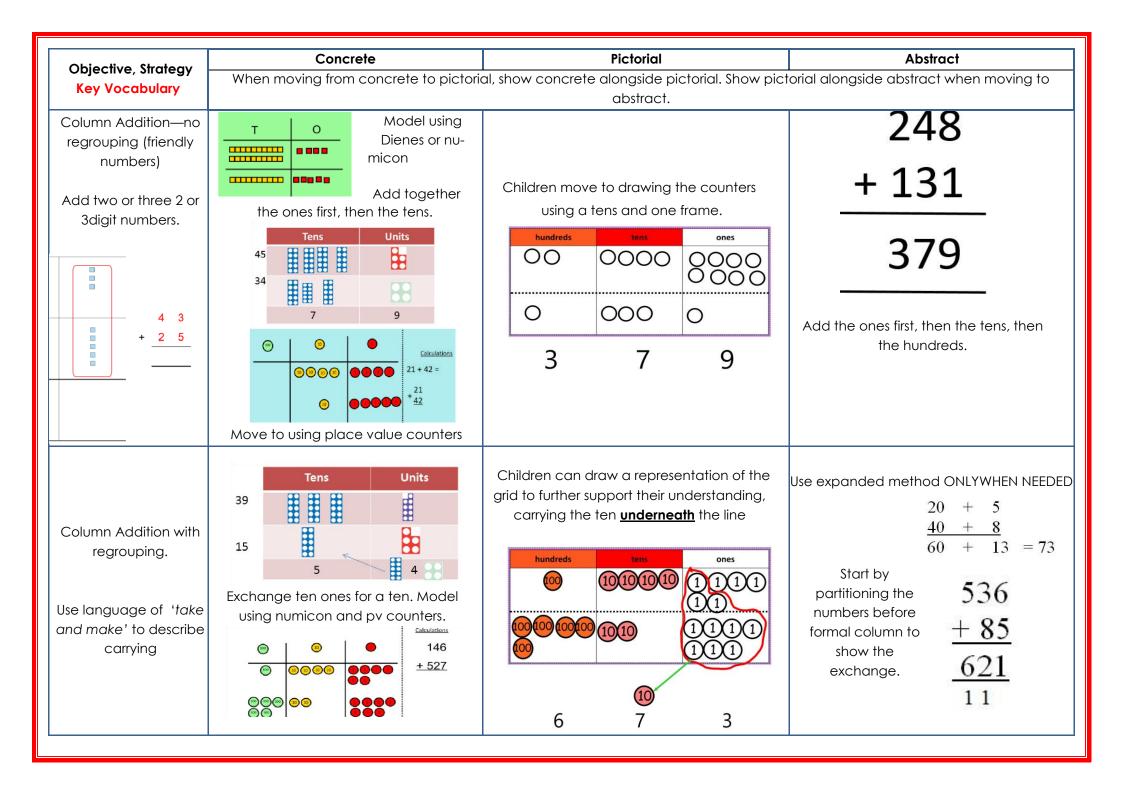
Objective, Strategy Key Vocabulary	Concrete	Pictorial	Abstract
Add a two digit number and ones	Use ten frame to make 'magic ten Children explore the pattern. $17 + 5 = 22$ $17 + 5 = 22$ $17 + 5 = 22$ $27 + 5 = 32$	Use part-part- whole and number line to model. 17 + 5 = 22 20 17 + 3 + 2 17 + 20 22	$ \begin{array}{c cccccccccccccccccccccccccccccccc$
Add a 2 digit number and tens	25 + 10 = 35 Explore that the ones digit does not change	25 + 30 = 55 +10 +10 +10 25 35 45 55	27 + 10 = 37 27 + 20 = 47 27 + \(\to = 57 \) \(\to + 30 = 67 \)
Add two 2-digit numbers without bridging. 'Friendly numbers'	Model using dienes , place value counters and numicon Dienes and part-part-whole model: 45	Use number line and bridge ten using part whole if necessary.	25 + 47 20 + 5

Objective, Strategy Key Vocabulary	Concrete	Pictorial	Abstract
Add any two 2-digit numbers	Dienes and part-part-whole model: 26 + 37 = 63 + 13 = 63	26 + 30 + 7 + 30 + 7 56 60 63 + 4 + 3	24 + 38 = $29 +$ $= 51$ $38 + 24 =$ $+ 22 = 51$
Add three 1-digit numbers	000	Use language of fist, then, then, now Pictorial: First Then Then Now	4+7+6=10+7 = 17
	Combine to make magic 10 first where relevant, or bridge 10 then add third	Use part part whole to show magic ten 2 + 3 + 8	Combine the two numbers that make/ bridge ten then add on the third.
Adding two numbers that bridge 10.	Use double sided counters and ten frames. Move counters to fill the ten frame and make Magic 10	Show on a number line how 5 is portioned into adding three, then adding 2.	7 + 5



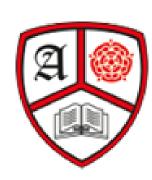
Year 3 Addition







Year 4-6 Addition

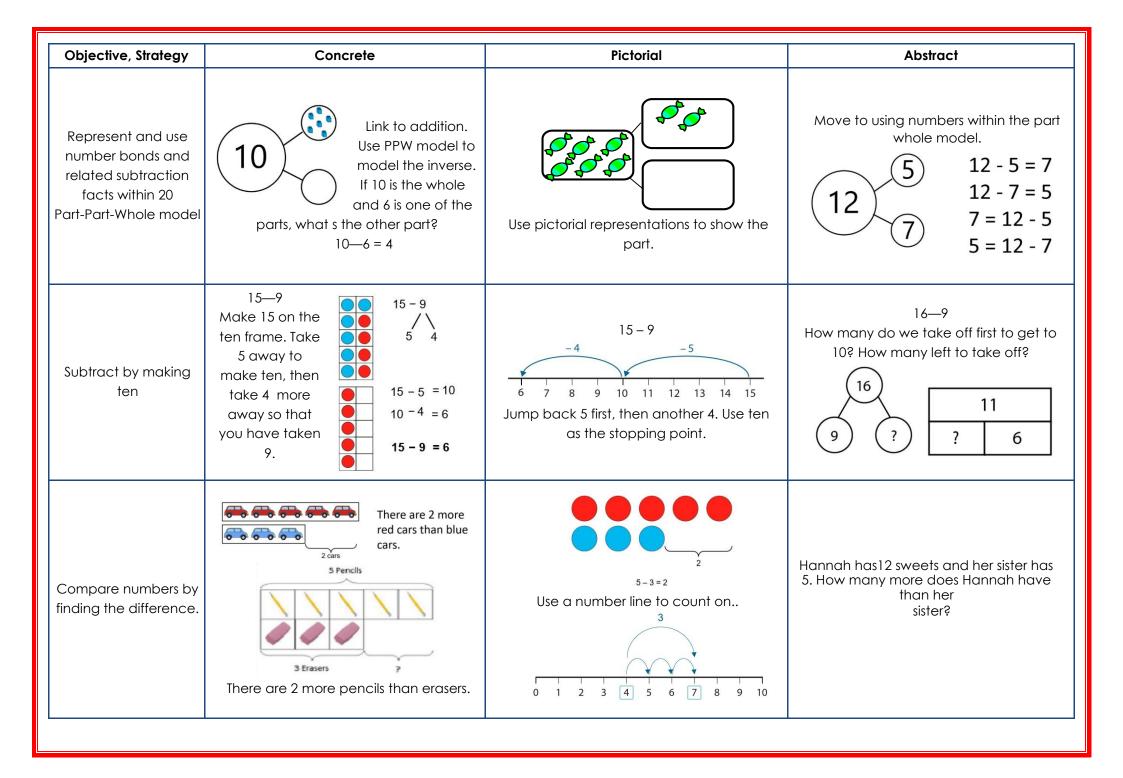


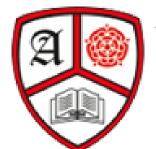
Objective ,Strategy Key Vocabulary	Concrete	Pictorial	Abstract
Y4—add numbers with up to 4 digits	Children continue to use dienes or pv counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand. Thousands hundreds ones ones ones ones ones ones ones one	7 1 5 1 Draw representations using pv grid.	2634 + 4517 7141 1 1 Continue from previous work to carry ones, tens and hundreds. Relate to money and measures.
Y5—add numbers with more than 4 digits. Add decimals with 2 decimal places, including money.	As year 4 ones tenths hundredths 1 1 01 01 01 01 01 01 01 01 01 01 01 01	2.37 + 81.79 tens ones tentes hundredites 00 000 0 00000 00000 0 00000 00000 0 00000 00000 0 00000	22,634 + 15,673 38,307 1 1 f 127.67 + f 38.45 f 166.12
Y6—add several numbers of increasing complexity Including adding money, measure and decimals with different numbers of decimal points.	Some children may need to ruse manipulatives and/or representations for longer. See year 5		$ \begin{array}{r} 89,472 \\ 63,673 \\ +3,016 \\ 156,161 \\ \hline 1 & 1 & 1 \\ 1 & 1 & 1 \\ \hline 1 & 1 & 1 \\ 1 & 1 & 1 \\ \hline 1 & 1 & 1 \\ 1 & 1 & 1 \\ \hline 1 &$



Year 1 Subtraction





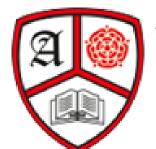


Year 2 Subtraction

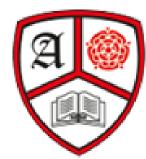


Objective & Strategy	Concrete	Pictorial	Abstract
Subtracting by making 10	15 - 9 =. Make 15 on the ten frame. Take 5 away to make ten, then take 4 more away so that you have taken 9. 15 - 9 =. 15 - 9 =. 15 - 9 = 10 15 - 5 = 10 10 - 4 = 6 15 - 9 = 6	15 - 9 = -4 -5 6 7 8 9 10 11 12 13 14 15 Jump back 5 first, then another 4. Use ten as the stopping point.	16 - 9 = How many do we take off first to get to 10? How many left to take off? 16 17 11 11 16 11 11 16 11 11
Counting on to next ten Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.	34 - 28 = 34—28 Use a bead bar or bead strings to model counting to next ten and the rest. 28 to 30 is 2, 30 to 34 is 4. So, 34 - 28 = 6	Use a number line to count on to next ten and then the rest. Begin with bead line, move to landmarked line then to ENL.	$ \begin{array}{c} $
Subtractions as difference	Ben is ten years old Charlotte is three years old 10 years old 3 years old difference of 7 years	7 4 3 3 0 1 2 3 4 5 6 7 8 9 10	The difference between 24 and 16 is 8.

Objective & Strategy	Concrete	Pictorial	Abstract
Subtracting a multiple of 10	32 - 10 = 22 Children use dienes, PV counters or Numicon. They remove the correct number of tens	Children draw rods and cubes and cross off multiples of ten.	64 - 10 =
Subtract a single digit from a two digit number No regrouping	9 29 3 6 3 26	-3 0 1 2 3 4 5 6 7 8 9 10 9 - 3 = 6 10 11 12 13 14 15 16 17 18 19 20 19 - 3 = 16	9 - 3 = 6 19 - 6 = 13 29 - 6 = 23 etc
Regroup a ten into ten ones	Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'.	20 - 4 = 16	20— 4 = 16
Partitioning to subtract without regrouping. 'Friendly numbers'	Use Dienes to show how to partition the number when subtracting without regrouping.	43—21 = 22 Children draw representations of Dienes and cross off.	43—21 = 22



Year 3 Subtraction



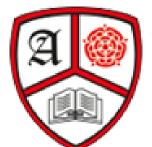
Objective & Strategy	Concrete	Pictorial	Abstract
Column subtraction without regrouping (friendly numbers)	47—32 Use base 10 or Numicon to model	Draw representations to support understanding	$47 - 24 = 23$ $-\frac{40 + 7}{20 + 3}$ Intermediate step may be needed to lead to clear subtraction understanding.
Column subtraction with regrouping	Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase 'take and make' for exchange.	Tens Ones 29 Tens Ones 20 20 20 20 20 20 20 20 20 2	$ \begin{array}{c} 836-254=582 \\ \hline 300-130-6 \\ -200-50-4 \\ \hline 500-80-2 \end{array} $ Begin by partitioning into pv columns $ \begin{array}{c} 728-582=146 \\ \hline 4-12-8 \\ \hline 1-4-6 \end{array} $ Then move to formal method.



Year 4 – 6 Subtraction

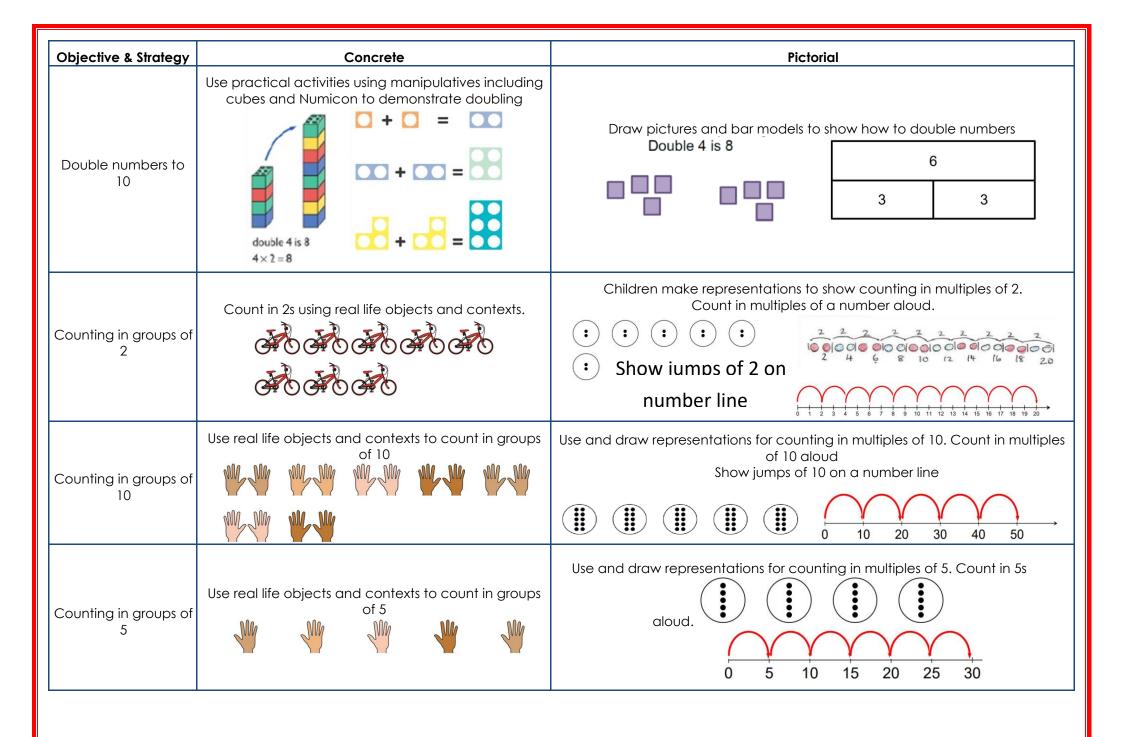


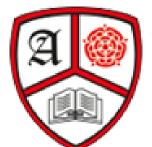
Objective & Strategy	Concrete	Pictorial	Abstract
Subtracting tens and ones Year 4 subtract with up to 4 digits. Introduce decimal subtraction through context of money	234 - 179	Children to draw pv counters and show their exchange—see Y3	2 x 5 4 - 1 5 6 2 1 1 9 2
	Model process of exchange using Numicon, base ten and then move to PV counters.		Use the phrase 'take and make' for exchange
Year 5- Subtract with at least 4 digits, including money and measures. Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal point.	As Year 4	Children to draw pv counters and show their exchange—see Y3	13 1 10 8 6 - 2 1 2 8 2 8 9 2 8 Use zeros for 17 16 9 0 - 3 7 2 5 6 7 9 6 5 5 placeholders.
Year 6—Subtract with increasingly large and more complex numbers and decimal values.			" " " " " " " " " " " " " " " " " " "



Year 1 Multiplication

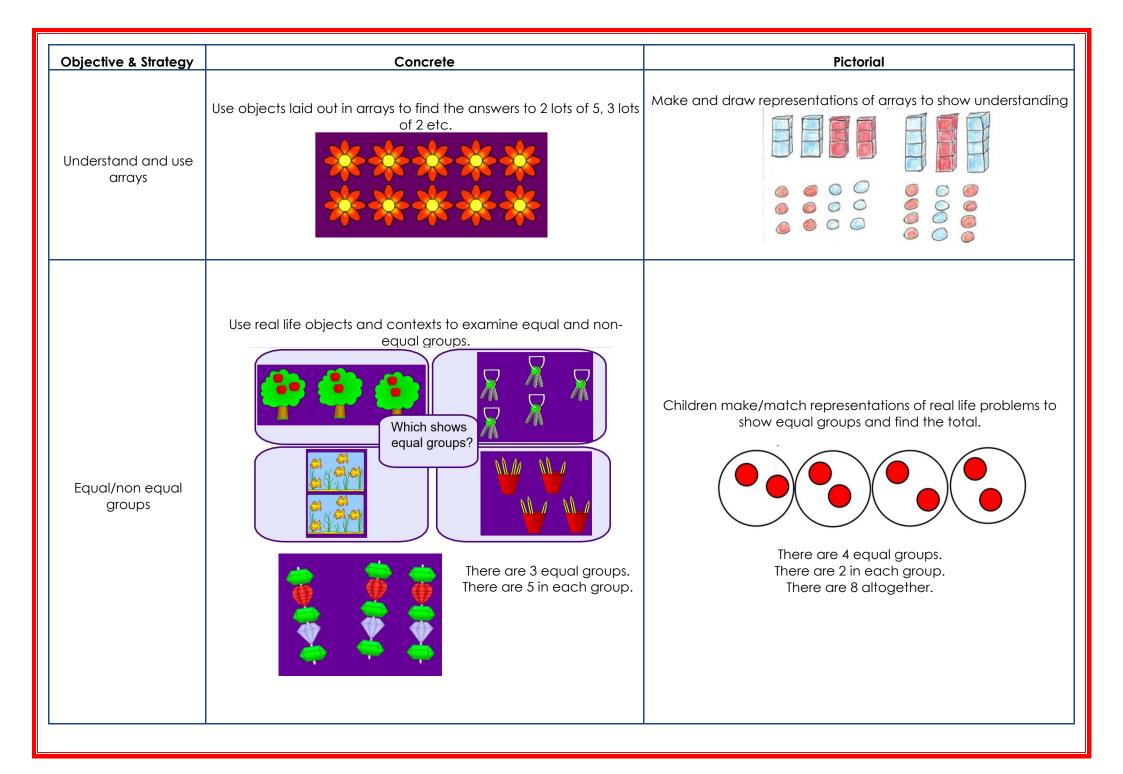




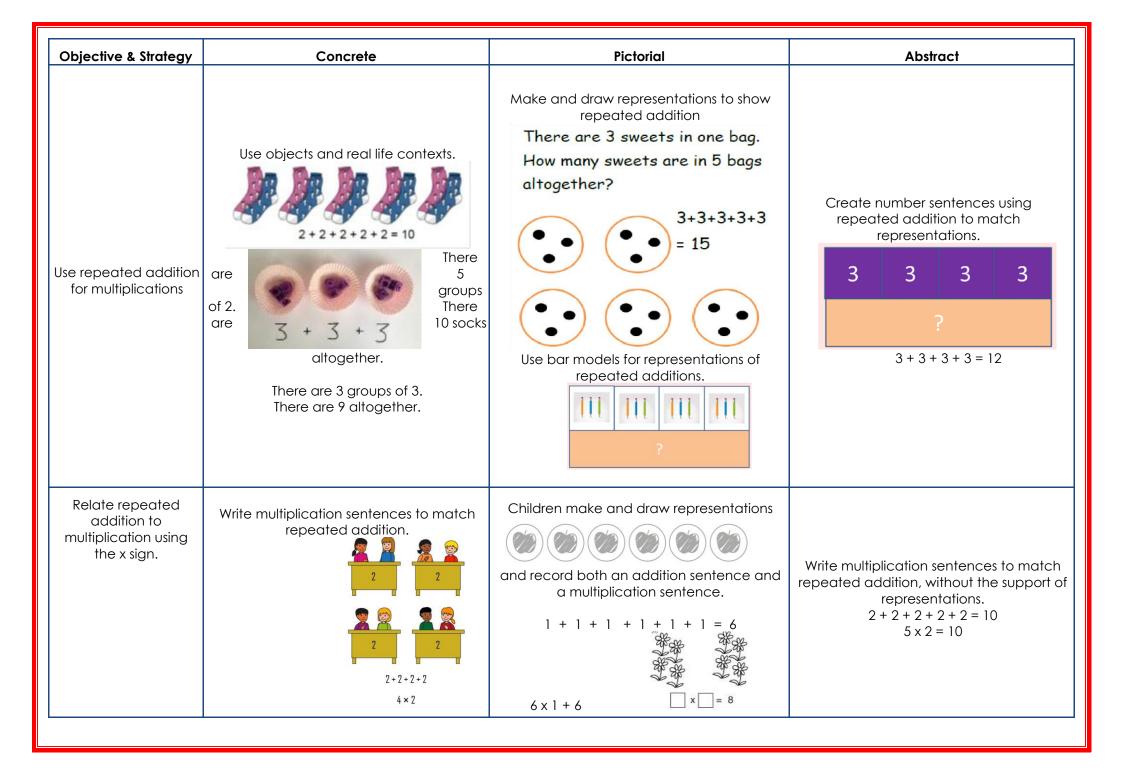


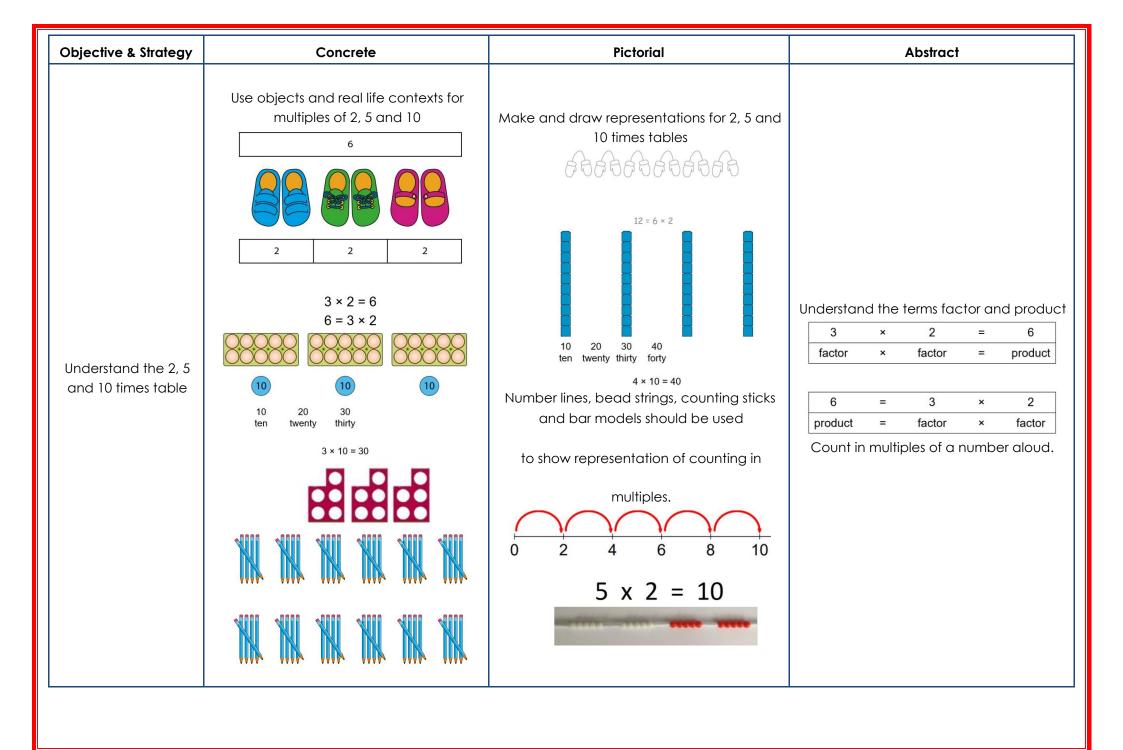
Year 2 Multiplication



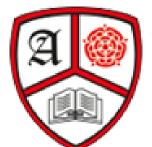


Objective & Strategy	Concrete	Pictorial	Abstract
Double a 2-digit number	Model doubling using dienes and PV counters. 40 + 12 = 52	Draw pictures and representations to show how to double numbers	Partition a number and then double each part before recombining it back together. 16 10 10 10 10 10 10 10 10 10
Understand equal and non-equal groups	There are 5 equal groups	Make representations and drawings of equal groups I have 4 groups of 3.	
	There are 5 equal groups. Each group has 3 cakes.		





Multiplication is commutative Create arrays using counters and cubes and Numicon. Use representations of arrays to show different calculations and explore commutativity. Use an array to write multiplication sentences and reinforce repeated addition. 5 + 5 + 5 = 15	commutative and Numicon. diffe	ifferent calculations and explore	
5 × 2 = 10 5 × 2 = 10 5 x 3 = 15 5 x 3 = 15 3 x 5 = 15 2, five times Fupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the	5 groups of 2 2 groups of 5 2, five times 5, two times	multiplication sentences and reinforce repeated addition. 00000 00000 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15



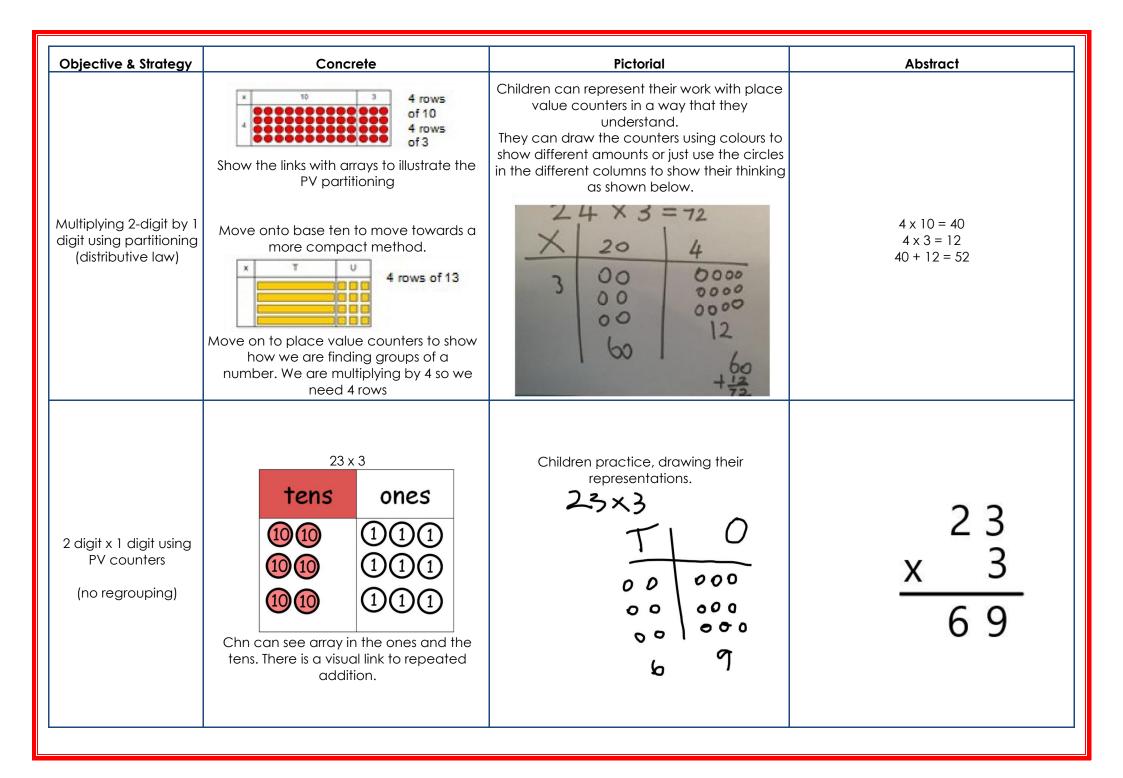
Year 3 Multiplication

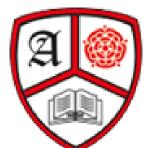


Objective & Strategy	Concrete	Pictorial	Abstract
Understand the 3 times table	Count in three using objects and representations of multiples of 3. 3 3 3	3 3 3 3 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	There are 12 wheels. 4 × 3 = 12 3 × 4 = 12
Understand the 6 times table	We can double our 3 times table to find our 6 times table. 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 <td>12 x 3 = 36 6 x 6 = 36</td>	12 x 3 = 36 6 x 6 = 36
Understand the 9 times table	Count in nines using objects and representations of multiples of 9. Make links 9 being three groups of three.	9 9 9 9 9	There are 36 apples. 4 × 9 = 36 9 × 4 = 36

Objective & Strategy	Concrete	Pictorial	Abstract
Understand the 4 times table	We can double our 2 times table to get the 4 times table 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	$12 \times 2 = 24$ $6 \times 2 = 24$ There are 20 wheels. $5 \times 4 = 20$ $4 \times 5 = 20$
Understand the 8 times table	We can double our 4 times table to get the 8 times table 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	24 4 4 4 4 4 4 8 8 8 6 fours 3 eights	6 x 4 = 24 3 x 8 = 24

Divisibility rules in 'families' - 2, 4 and 8		
2	A number is divisible by 2 if the ones digit is	
	even.	
4	If halving a number gives an even value, then	
	the number is divisible by 4.	
	and	
	For numbers with more than two digits: if the	
	final two digits are divisible by 4 then the	
	number is divisible by 4.	
8	If halving a number twice gives an even value,	
	the number is divisible by 8.	

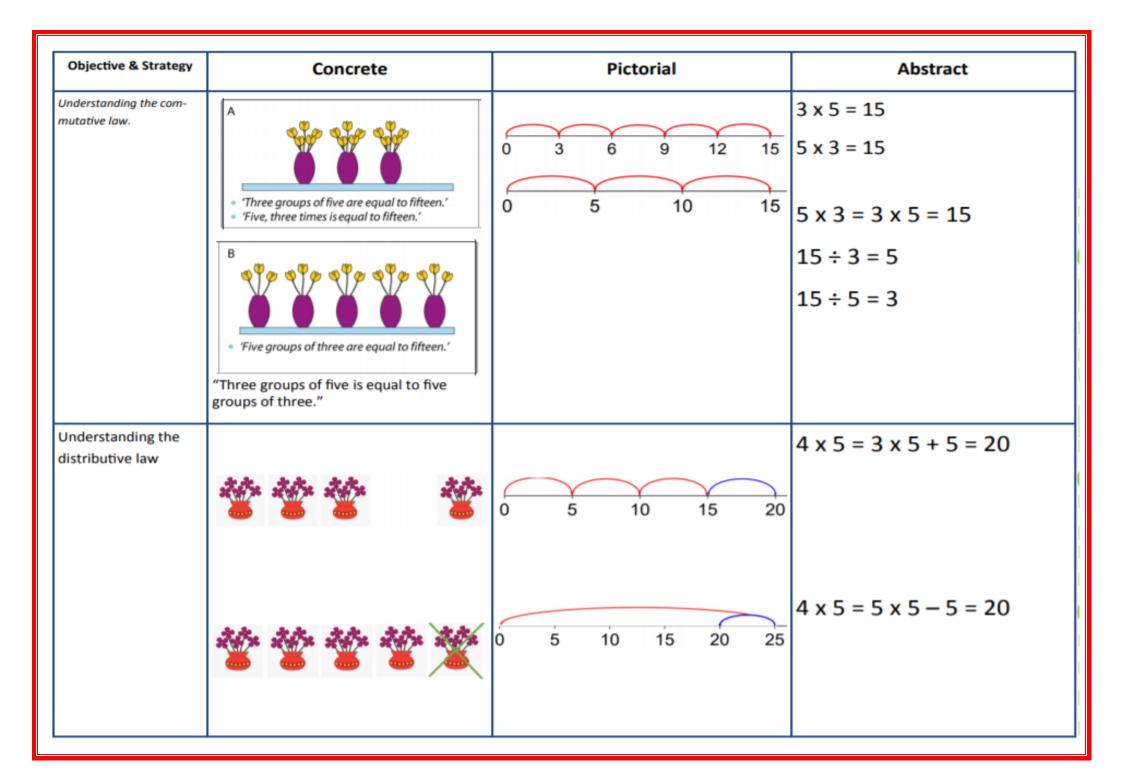




Year 4 Multiplication



Objective & Strategy	Concrete	Pictorial	Abstract
Understand the 7 times table	Children use representations which show The last set of the set o	Linear models show jumps of 7.	There are 14 players. 2 × 7 = 14 7 × 2 = 14



Objective & Strategy	Concrete	Pictorial	Abstract
Multiply 3 digit numbers by 1 digit. (no exchange)	Use place value counters to show how we are finding groups of a number. We are multiplying by 3 so we need 3 rows 123 x3 = 369 hundreds tens ones 100 0 0 0 0 0 0 300 + 60 + 9 Add up each column, starting with the ones.	Children can represent their work with place value counters by drawing place value counters or Dienes.	231 3 x 1 ones is three ones 3 x 3 tens is nine tens 3 x 2 hundreds is six hundreds
Multiply 3 digit numbers by 1 digit. (with exchange)	224 x 3 hundreds tens ones	H T D 00 00000 0 H T D 00 00000 0 00 00000 0 500 + 20 + 2 =522	4 times 1 ones is 4 ones 4 times 1 ones is 4 ones 4 times 4 tens is 16 tens. I put 6 tens down and carry ten tens which is now a hundred. 4 times 2 hundreds is 8 hundreds. I add the hundred I have carried to make 9 hundreds.



Year 5 Multiplication



Objective & Strategy	Concrete	Pictorial	Abstract
Multiply 3 and 4 digits x 1 digit.	Children may continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. 3024 x 3 Thousands bundreds ones ones ones ones ones ones ones one	Children may continue to draw their understanding using place value grids.	3024 x 3 9072
Multiply up to 4 digits by 2 digits	Manipulatives may still be used with the corresponding long multiplication modelled alongside. Begin with teen number x teen number. Progress to any 2 –4 digit number x 2 digit.	10 100 80 30 24	18 x 3 on the first row (8 x 3 = 24, carrying the 2 for 20, then 1 x 3) 18 x 10 on the 2nd row. Show multiplying by 10 by putting zero in units first x



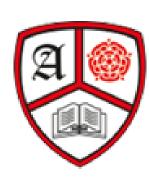
Year 6 Multiplication

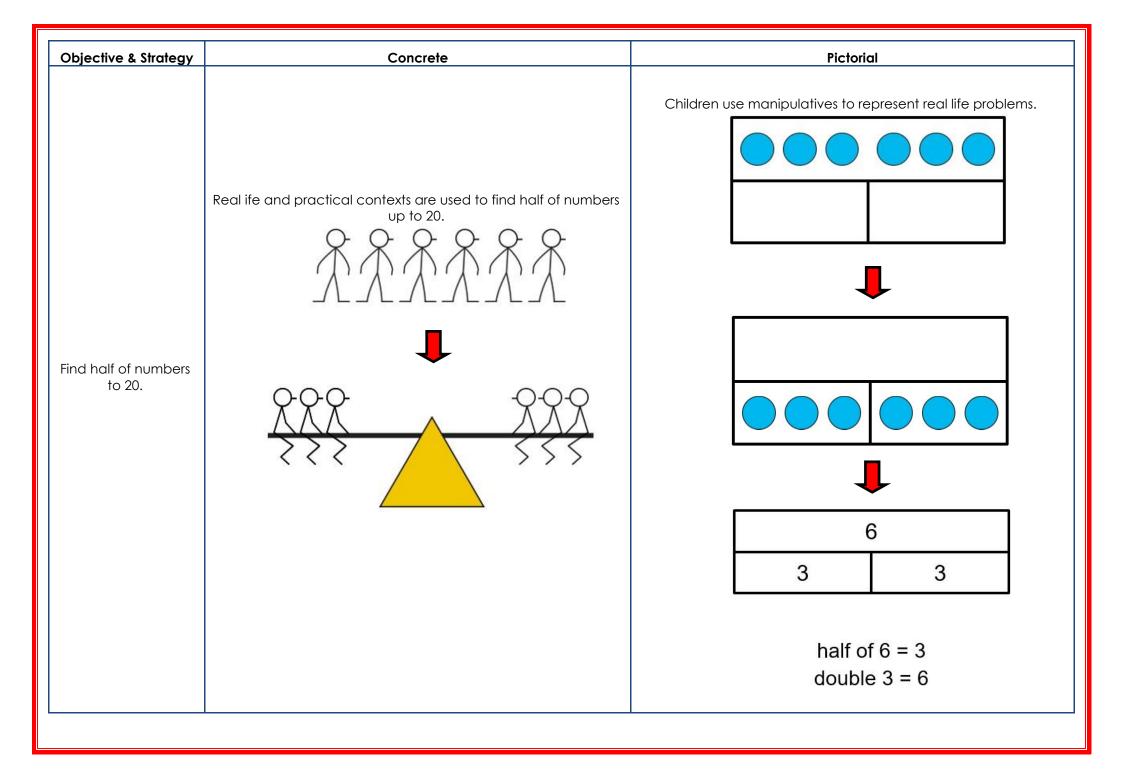


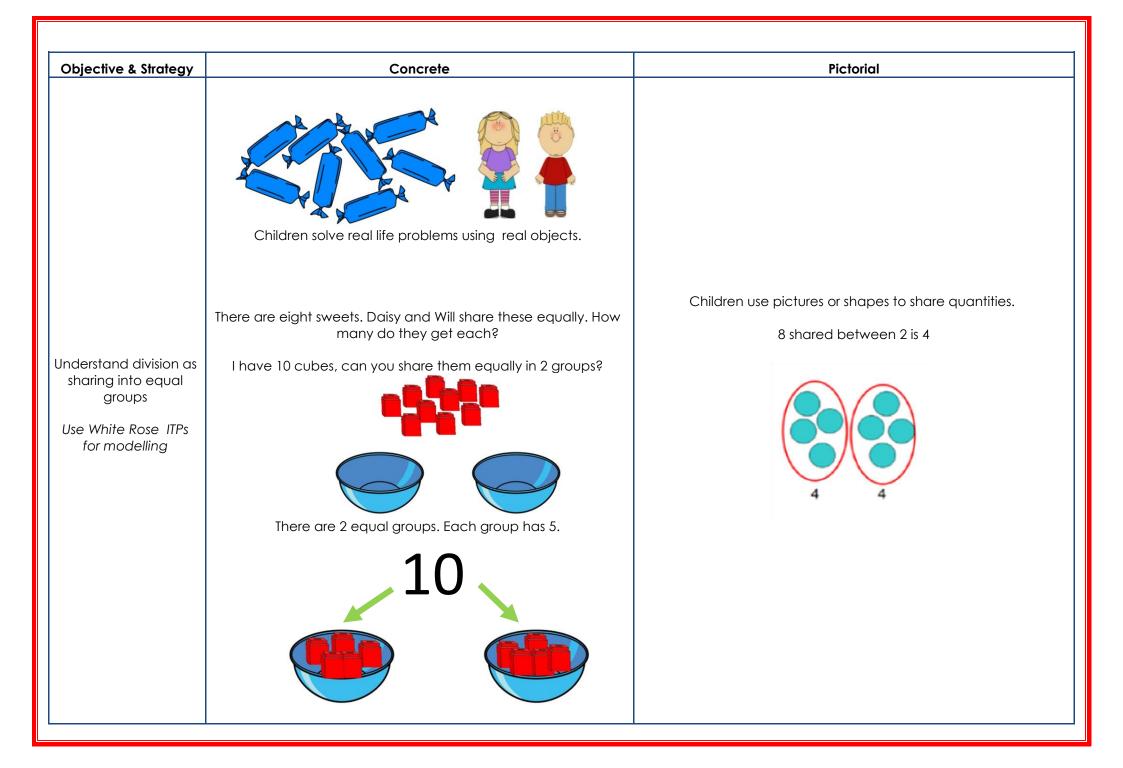
Objective & Strategy	Concrete	Pictorial	Abstract
Multiply decimals up to2 decimal places by a single digit			2.38 x 3 714 12 First we lay out the calculation Next, we write the decimal point in the answer (product). Finally, we carry out the multiplication. 3 x 8 hundredths is 24 hundredths 3 x 3 tenths is 9 tenths, add 2 tenths we carried is 11 tenths 3 x 3 ones is 6 ones, add 1 one we carried is 7 ones
Multiply up to 4 digit numbers by 2 digits.			3 1 2 × 2 8 2 4 9 6 6 2 4 0 8 7 3 6 1

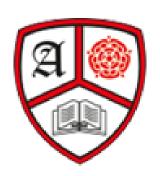


Year 1 Division







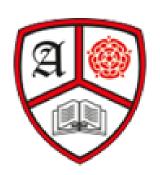


Year 2 Division

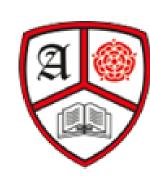


Objective & Strategy	Concrete	Pictorial	Abstract
Division as sharing (partitive)	There are 20 conkers shared equally between 5 children. Each child gets 4 conkers.	Children use pictures or shapes to share quantities. They may use bar modelling to show and support understanding. 4 fives 20 Number lines are used to show skip counting (counting forwards) and repeated subtraction (counting backwards). -5 -5 -5 -5 -5 -5 -5 -5 -5 -5 -5 -5 -5	20 ÷ 5 = 4
Division as grouping (quotitive)	Use cubes, counters or real objects or to aid understanding. There are 15 biscuits, there are 5 in each bag. How many bags?		15 divided into groups of 5 is 3

	Understanding the inverse 0	Objective & strategy	Concrete	Pictorial	Abstract
Understanding the linear section in the section $\frac{12 \div 4 = 3}{4}$ $\frac{4 \times 3 = 12}{12 \div 3 = 4}$		Understanding the		X	12 ÷ 4 = 3 4 x 3 = 12 12 ÷ 3 = 4 2 x 4 = 8



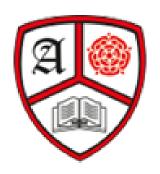
Year 3 Division



Objective & Strategy	Concrete	Pictorial	Abstract
Division with remainders. (partitive)	I divide 14 cakes between 3 plates. How are the cakes shared?	Draw dots and group them to divide an amount and clearly show a remainder.	Complete written divisions and show the remainder using r. 14 ÷ 3 = 4 r 2 dividend divisor quotient remainder
Division with remainders. (quotitive)	13 eggs are put into boxes. Each box holds 3 eggs. How are the eggs boxed?	Children may draw representations to show their understanding. Use bar models to show division with remainders. 13 3 3 3 3 1	13 ÷ 3 = 4 r 1

Divis	sibility rules in 'families' – 3, 6 and 9
3	For a number to be divisible by 3, the sum of the digits of the number must be divisible by 3.
6	For a number to be divisible by 6, the number must be divisible by both 2 and 3.
9	For a number to be divisible by 9, the sum of the digits of the number must be divisible by 9.

Divis	sibility rules in 'families' – 5 and 10
5	A number is divisible by 5 if the ones digit is
	5 or 0.
10	A number is divisible by 10 if the ones digit
	is 0.



Year 4 Division



Objective & Strategy	Concrete	Pictorial	Abstract
Interpreting division with remainders.	Bracelets are made using 4 beads. There are 23 beads. How many bracelets can be made? How many beads left over?	Bar model representations may be used. 23 4 4 4 4 4 3	23 ÷ 4 = 5 r 3
Interpreting division with remainders.	4 scouts can fit in each tent. How many tents needed for 30 scouts? 4 4 4 4 4 4 4 4 4 4	30 4 4 4 4 4 4 2	30 ÷ 4 = 7 r 2 8 tents are needed. Discuss with pupils the need to round up in this context.

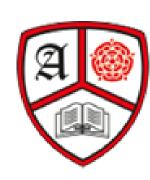
Objective & Strategy	Concrete	Pictorial	Abstract
Divide 2 & 3 digit numbers by 1 digit Short Division	Use place value counters to make groups of the divisor, starting with the largest value digit. 3 2 3 10 10 10 10 1 1 1 1 1 1 1 There are 3 groups of 3 tens. There are 2 groups of 3 ones. 42 ÷ 3 42 ÷ 3 There is 1 group of 3 tens. There is a ten left over. We exchange this for 10 ones. 12 ones divided by 3 is 4. 432 ÷ 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 4 1 0 8 5 1 9 10 10 10 10 10 10 10 10 10 10 10 10 10	Students use drawn diagrams with spots or circles to show their understanding.	Begin with divisions that divide equally with no remainder. 124 372 Move on to divisions with a remainder. Return to concrete if necessary. 138 r3 4527

Divis	ibility rules in numerical order
2	A number is divisible by 2 if the ones digit is even.
3	For a number to be divisible by 3, the sum of the digits of the number must be divisible by 3.
4	If halving a number gives an even value, then the number is divisible by 4. and For numbers with more than two digits: if the final two digits are divisible by 4 then the number is divisible by 4.
5	A number is divisible by 5 if the ones digit is 5 or 0.

Divisibility rules in numerical order			
6	For a number to be divisible by 6, the number must		
	be divisible by both 2 and 3.		
8	If halving a number twice gives an even value, the		
	number is divisible by 8.		
9	For a number to be divisible by 9, the sum of the		
	digits of the number must be divisible by 9.		
10	A number is divisible by 10 if the ones digit is 0.		



Year 5 Division



Objective & Strategy	Concrete	Pictorial	Abstract
Divide decimals by a single digit, using x and ÷ by 10 or 100			Pupils understand the use of X and \div 10 to make connections. 6.3 \div 9 = 0.7 \star 10 6.3 \div 9 = 7
Short division of decimals			Children build on work from Year 4, now with decimals. 0 · 4 · 1 6)2 · ² 4 6

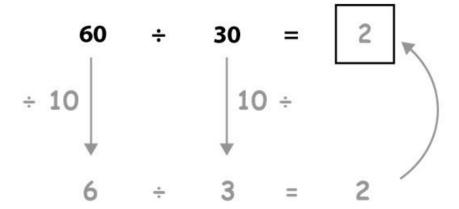


Year 6 Division



Division of 2 digits by 2 digits

Using $x \& \div$ by 10, 100 etc and relating this to a short division method.



Long Division—2 digits divided by 2 digits

T O

30 does not go into 8. So, combine the 8

tens with the 5 ones.

Subtract the 60 from

the 85 and this leaves

25.

(

2

30)8 5

50

30 goes into 85 twice, which is 60.

T O

2

5

6 0

2 5

Γ

2 r 25

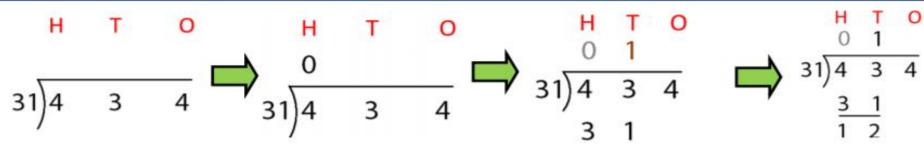
0)8 5

6 0

2 5

85 divided by 30 is 2 with a remainder of 25

Long Division—3 digits divided by 2 digits



31 does not go into 4 (hundreds).

We combine the 4 hundreds with the tens to give 43 tens. 31 goes into 43 once which is 31, we record this underneath.

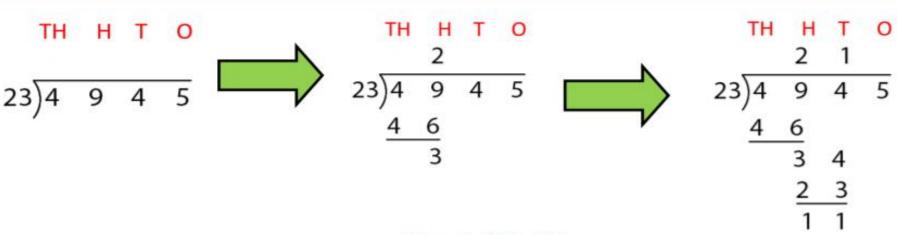
Subtract to find the remainder. 31 from 43 leaves 12.

We combine 12 with the next digit to give 124.

31 goes into 124 four times, which is 124.

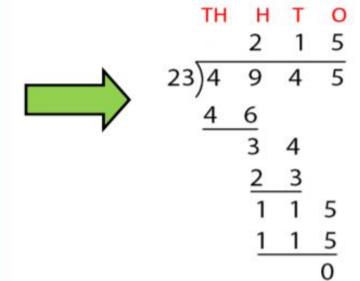
We subtract to show there is no remainder

Long Division—progressing to 4 or more digits



23 goes into 49 twice which is 46. We subtract this from 49 to give a remainder of 3.

We combine the 3 left over with the next digit to give 34. 23 goes into 34 once with 11 remaining.



We combine the 11 with the next digit to make 115. 23 goes into 115 5 times with no remainder.

Long Division—procedural summary (remainder in the tens)

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2) 5 8	2 2)58 -4 1	2 9 2) 5 8 - 4 1 1 8
Two goes into 5 two times, or 5 tens + 2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
t o	t o	t o
2 9 2) 5 8	29	2)58
- <u>4</u> 1 8	<u>- 4</u> 1 8	<u>-4</u> 18
	<u>- 1 8</u> 0	<u>- 1 8</u> 0
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.

Long Division—procedural summary (remainder in any of the digits)

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 2)278	2)278 -20	18 2)278 -2↓ 07
Two goes into 2 one time, or 2 hundreds ÷ 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
13 2)278 -2 07	13 2)278 -2 07 -6	13 2)278 -2 07 -6 18
Divide 2 into 7. Place 3 into the quotient.	Multiply $3 \times 2 = 6$, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
13 <mark>9</mark> 2)278 -2 07 -6	139 2)278 -2 07 -6 18 -18	139 2)278 -2 07 -6 18 -18
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract to find the remainder of zero.	There are no more digits to drop down. The quotient is 139.