Anderton Primary School Maths Mastery Calculation Policy

Date for next review:
Signed :
Signed :


| Objective, Strategy <br> Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Comparing Objects, groups of objects Length, weight, mass, heavier, lighter, same, equal | People's height, distance, mass. <br> Use of pan balances using Numicon or similar to show equivalence, < > Comparing multiple objects <br> Use of concrete materials eg. Compare bears, jewels, cubes etc to create groups of different sizes to compare |  |  |
| Using $<>$ and $=$ <br> Fewer, more, less than, more than, equal to, fewer than | Use a multilink staircase in two colours |  | Use variation with missing boxes and missing symbols. $\begin{aligned} & 3 \bigcirc 4 \\ & 2 \bigcirc 2 \\ & 2 \bigcirc 2 \\ & 2<6 \end{aligned}$ |
| Finding one more, finding one less |  |  | One more/less sentences - example one: <br> 1 more than 3 is $\square$ <br> 1 less than 2 is $\square$ <br> 1 more than $\square$ is 1 <br> 1 less than $\square$ is 1 |


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| :---: | :---: | :---: | :---: | :---: | :---: |
| Adding 1 gives 1 more |  | Then | Now | 6 |  |
| Augmentationincreasing an amount | Use FIRST, THEN, NOW and range of practical situations for showing augmentation. <br> E.g. first there were three chn on carpet then 2 more came. Now there are 5 chn on the carpet. |  |  | 4 |  |
| Stories of numbers within 10 | Children should work with doubled sided counters and ten frame. <br> Start with 7 red, turn one over, tell me the 'story'? <br> Turn one more over. What is the 'story'? <br> Continue. <br> Complete this for stories of all numbers up to <br> 10. |  | $\begin{aligned} & 7+0=7 \\ & 6+1=7 \\ & 5+2=7 \\ & \text { efic } \end{aligned}$ <br> Complete for all numbers up to 10 |  | $\begin{aligned} & 7+0=7 \\ & 6+1=7 \\ & 5+2=7 \\ & 4+3=7 \\ & 3+4=7 \\ & 2+5=7 \\ & 1+6=7 \\ & 0+7=7 \end{aligned}$ |


| Objective, Strategy <br> Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Combining two parts to make a whole: partwhole model | Use part part whole model. <br> Use cubes to add two <br> numbers together as a group or in a bar. | Use pictures to add two numbers together | 5 <br> 3 $4+3=7$ $10=6+4$ <br> Use the part whole diagram as shown above to move into the abstract. |
| Regrouping to make $10 .$ <br> This is an essential skill for column addition later. | cepecece <br>  <br> 2 more than 5 . | Start at the larger number on the number line and count on in ones or in one jump to find the answer. | $7+4=11$ <br> If I am at seven, how many more do I need to make 10. How many more do I add on now? |
| Represent \& use number bonds and related subtraction facts within 20 | Start with the bigger number and use the smaller number to make 10. <br> Use ten frame | Use pictures or a number line. Regroup or partition the smaller number using the part whole model to make 10. $9+5=14$ <br> 14 | Emphasis should be on the language <br> ' 1 more than 5 is equal to 6 .' <br> '2 more than 5 is 7. ' ' 8 <br> is 3 more than 5 .' |


| + | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | $0+0$ | $0+1$ | $0+2$ | $0+3$ | $0+4$ | $0+5$ | $0+6$ | $0+7$ | $0+8$ | $0+9$ | $0+10$ |
| 1 | $1+0$ | $1+1$ | $1+2$ | $1+3$ | $1+4$ | $1+5$ | $1+6$ | $1+7$ | $1+8$ | $1+9$ | $1+10$ |
| 2 | $2+0$ | $2+1$ | $2+2$ | $2+3$ | $2+4$ | $2+5$ | $2+6$ | $2+7$ | $2+8$ | $2+9$ | $2+10$ |
| 3 | $3+0$ | $3+1$ | $3+2$ | $3+3$ | $3+4$ | $3+5$ | $3+6$ | $3+7$ | $3+8$ | $3+9$ | $3+10$ |
| 4 | $4+0$ | $4+1$ | $4+2$ | $4+3$ | $4+4$ | $4+5$ | $4+6$ | $4+7$ | $4+8$ | $4+9$ | $4+10$ |
| 5 | $5+0$ | $5+1$ | $5+2$ | $5+3$ | $5+4$ | $5+5$ | $5+6$ | $5+7$ | $5+8$ | $5+9$ | $5+10$ |
| 6 | $6+0$ | $6+1$ | $6+2$ | $6+3$ | $6+4$ | $6+5$ | $6+6$ | $6+7$ | $6+8$ | $6+9$ | $6+10$ |
| 7 | $7+0$ | $7+1$ | $7+2$ | $7+3$ | $7+4$ | $7+5$ | $7+6$ | $7+7$ | $7+8$ | $7+9$ | $7+10$ |
| 8 | $8+0$ | $8+1$ | $8+2$ | $8+3$ | $8+4$ | $8+5$ | $8+6$ | $8+7$ | $8+8$ | $8+9$ | $8+10$ |
| 9 | $9+0$ | $9+1$ | $9+2$ | $9+3$ | $9+4$ | $9+5$ | $9+6$ | $9+7$ | $9+8$ | $9+9$ | $9+10$ |
| 10 | $10+0$ | $10+1$ | $10+2$ | $10+3$ | $10+4$ | $10+5$ | $10+6$ | $10+7$ | $10+8$ | $10+9$ | $10+10$ |



| Objective \& Strategy <br> \& Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Adding multiples of ten | Model using dienes and bead strings | $\qquad$ tens and $\qquad$ tens <br> makes $\qquad$ tens <br> Use representations for base ten. | $\begin{aligned} & 20+30=50 \\ & 70=50+20 \\ & 40+\square=60 \\ & \square+30=50 \end{aligned}$ |
| Use known number facts <br> Part part whole | Children explore ways of making numbers within 20 | $\begin{gathered} 20-\square \\ \square+\square=20 \quad 20-\square=\square \\ \square+\square=20 \quad 20-\square=\square \end{gathered}$ | $\begin{array}{ll} \square+1=16 & 16-1=\square \\ 1+\square=16 & 16-\square=1 \end{array}$ |
| Using known facts |  | Children draw representations of $\mathrm{H}, \mathrm{T}$ and O | $3+4=7$ <br> Leads to $30+40=70$ <br> Leads to $300+400+700$ <br> ' 3 things and 4 things is always 7 things' |
| Bar model |  | $8$ | 30 |
|  | $3+4=7$ | $3+5=8$ | $14+16=30$ |


| Objective, Strategy <br> Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Add a two digit number and ones | $17+5=22$ <br> Use ten frame to make 'magic ten Children explore the pattern. $17+5=22$ $27+5=32$ | Use part-partwhole and number line to model. |  22  <br>  $5+5=22$  <br>  17  <br> Explore related   <br> $17+5=22$   <br>    <br>  $17+5$  <br> $5+17=22$  $22=5+17$ <br> $22-17=5$  $17=22-5$ <br> $22-5=17$  $5=22-17$ |
| Add a 2 digit number and tens | $25+10=35$ <br> Explore that the ones digit does not change |  | $\begin{aligned} 27+10 & =37 \\ 27+20 & =47 \\ 27+\square & =57 \\ \square+30 & =67 \end{aligned}$ |
| Add two 2-digit numbers without bridging. <br> 'Friendly numbers' | Model using dienes, place value counters and numicon Dienes and part-part-whole model: | Use number line and bridge ten using part whole if necessary. | $\begin{gathered} 25+47 \\ 20+5 \quad 40+7 \\ 20+40=60 \\ 5+7=12 \\ 60+12=72 \end{gathered}$ |


| Objective, Strategy Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Add any two 2-digit numbers | Dienes and part-part-whole model: | $26+30+7$ | $24+38=$ $\square$ $29+$ $\square$ $=51$ $38+24=$ $\square$ $\square$ $+22=51$ |
| Add three 1-digit numbers | Combine to make magic 10 first where relevant, or bridge 10 then add third | Use language of fist, then, then, now Pictorial: <br> Use part part whole to show magic ten | $\begin{aligned} \frac{4+7}{10} & =10+7 \\ & =17 \end{aligned}$ <br> Combine the two numbers that make/ bridge ten then add on the third. |
| Adding two numbers that bridge 10 . | Use double sided counters and ten frames. Move counters to fill the ten frame and make Magic 10 | Show on a number line how 5 is portioned into adding three, then adding 2. |  |



| Objective, Strategy Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
|  | When moving from concrete to pictorial, show concrete alongside pictorial. Show pictorial alongside abstract when moving to abstract. |  |  |
| Column Addition-no regrouping (friendly numbers) <br> Add two or three 2 or 3digit numbers. | Move to using place value counters | Children move to drawing the counters using a tens and one frame. | $\begin{array}{r} 248 \\ +131 \\ \hline 379 \\ \hline \end{array}$ <br> Add the ones first, then the tens, then the hundreds. |
| Column Addition with regrouping. <br> Use language of 'take and make' to describe carrying | Exchange ten ones for a ten. Model using numicon and pv counters. | Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line | Use expanded method ONLYwhen needed |



| Objective , Strategy Key Vocabulary | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Y4—add numbers with up to 4 digits | Children continue to use dienes or pv counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand. | $\bullet$ $\ddots$ $\bullet$ $\because$  <br> $\because \bullet$ $\bullet \bullet$ $\bullet$ $\ddots$  <br>  $\ddots \bullet$  $\bullet$  <br> 7 1 5 1  <br> $\bullet$ $\bullet$    <br> Draw representations using pv grid. | $\begin{array}{r} 2634 \\ +4517 \\ \hline 7141 \\ \hline 11 \end{array}$ <br> Continue from previous work to carry ones, tens and hundreds. Relate to money and measures. |
| Y5-add numbers with more than 4 digits. <br> Add decimals with 2 decimal places, including money. | As year 4 <br> Introduce decimal place value counters |  |  |
| Y6-add several numbers of increasing complexity <br> Including adding money, measure and decimals with different numbers of decimal points. | Some children may need to ruse manipulatives and/or representations for longer. See year 5 |  |  |



| Objective, Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Represent and use number bonds and related subtraction facts within 20 Part-Part-Whole model | Link to addition. <br> Use PPW model to model the inverse. If 10 is the whole and 6 is one of the parts, what $s$ the other part? $10-6=4$ | Use pictorial representations to show the part. | Move to using numbers within the part whole model. $\begin{aligned} & 12-5=7 \\ & 12-7=5 \\ & 7=12-5 \\ & 5=12-7 \end{aligned}$ |
| Subtract by making ten | 15-9 <br> Make 15 on the ten frame. Take 5 away to make ten, then take 4 more away so that you have taken 9. <br> 15-9 $\begin{aligned} & 15-5=10 \\ & 10-4=6 \\ & 15-9=6 \end{aligned}$ | $15-9$ <br> Jump back 5 first, then another 4 . Use ten as the stopping point. | $16-9$ <br> How many do we take off first to get to 10? How many left to take off? |
| Compare numbers by finding the difference. | There are 2 more pencils than erasers. | $5-3=2$ <br> Use a number line to count on.. | Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister? |



| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Subtracting by making 10 | 15-9 =. <br> Make 15 on the ten frame. Take 5 away <br> 15-9 to make ten, then take 4 more away so that you have <br> $15-5=10$ <br> $10^{-4}=6$ <br> $15-9=6$ | Jump back 5 first, then another 4. Use ten as the stopping point. | $16-9=$ <br> How many do we take off first to get to 10? How many left to take off? <br> ? |
| Counting on to next ten <br> Progression should be crossing one ten, crossing more than one ten, crossing the hundreds. | $34-28=$ $34-28$ <br> Use a bead bar or bead strings to model counting to next ten and the rest. <br> 28 to 30 is 2,30 to 34 is 4 . So, $34-28=6$ | Use a number line to count on to next ten and then the rest. <br> Begin with bead line, move to landmarked line then to ENL. |  |
| Subtractions as difference |  |  | The difference between 24 and 16 is 8. |


| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Subtracting a multiple of 10 | $32-10=22$ <br> Children use dienes, PV counters or Numicon. They remove the correct number of tens | $\left\|\left\|\|\|c\| c c\| \begin{array}{cc} 0 & 0 \\ 0 & \begin{array}{l} \text { Children draw } \\ \text { rods and cu- } \\ 0 \end{array} \\ \text { bes and cross } \\ \text { off multiples } \\ \text { of ten. } \end{array}\right.\right.$ | $\begin{aligned} & 64-10=\square \\ & 64-20=\square \\ & 64-30=\square \\ & 64-\square=24 \\ & \square-50=14 \end{aligned}$ |
| Subtract a single digit from a two digit number <br> No regrouping |  | $9-3=6$ $19-3=16$ | $\begin{gathered} 9-3=6 \\ 19-6=13 \\ 29-6=23 \text { etc } \end{gathered}$ |
| Regroup a ten into ten ones | Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'. | $20-4=16$ | $20-4=16$ |
| Partitioning to subtract without regrouping. 'Friendly numbers' | $34-13=21$ <br> Use Dienes to show how to partition the number when subtracting without regrouping. | $43-21=22$ <br> Children draw representations of Dienes and cross off. | $43-21=22$ |



| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Column subtraction without regrouping (friendly numbers) | $47-32$ <br> Use base 10 or Numicon to model |  | $\begin{gathered} 47-24=23 \\ -40+7 \\ -\frac{20+4}{20+3} \\ \hline \end{gathered}$ <br> Intermediate step may be needed to lead to clear subtraction understanding. |
| Column subtraction with regrouping | Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into tten ones. Use the phrase 'take and make' for exchange. | Children may draw base ten or PV counters and cross off. |  <br> Begin by partitioning into pv columns $\begin{array}{ccc} 728 & -582=146 \\ \hline 1 & 9 & 4 \\ { }^{\prime} 7 & 2 & 8 \\ 5 & 8 & 2 \\ \hline 1 & 4 & 6 \end{array}$ <br> Then move to formal method. |



| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Subtracting tens and ones <br> Year 4 subtract with up to 4 digits. <br> Introduce decimal subtraction through context of money | 234-179  <br> Model process of exchange using Numicon, base ten and then move to PV counters. | Children to draw pv counters and show their exchange-see Y3 | Use the phrase 'take and make' for exchange |
| Year 5-Subtract with at least 4 digits, including money and measures. <br> Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal point. | As Year 4 | Children to draw pv counters and show their exchange-see Y3 | $\begin{array}{r} { }^{2} 8^{10} x^{1} 0{ }^{\circ} 8^{\prime} 6 \\ -\quad 2128 \\ \hline 28,928 \end{array}$ <br> Use zeros for $\begin{array}{r} 67^{10} x^{8} 9 \cdot 0 \\ -\quad 372 \cdot 5 \\ \hline 6796.5 \end{array}$ <br> placeholders. |
| Year 6-Subtract with increasingly large and more complex numbers and decimal values. |  |  | $\begin{array}{r} { }^{146} 8 \not 6,699 \\ -89,949 \\ \hline 60,750 \\ \hline \begin{array}{r} 1085 \cdot 3 \end{array} \\ \hline 36 \cdot 089 \mathrm{~kg} \\ \hline 69 \cdot 339 \mathrm{~kg} \end{array}$ |





| Objective \& Strategy |  |
| :--- | :--- | :--- | :--- | :--- | Use objects laid out in arrays to find the answers to 2 lots of 5 , 3 lots


| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Double a 2-digit number | Model doubling using dienes and PV counters. $40+12=52$ | Draw pictures and representations to show how to double numbers | Partition a number and then double each part before recombining it back together. |
| Understand equal and non-equal groups | These are non- equal groups <br> There are 5 equal groups. Each group has 3 cakes. | Make representations and drawings of equal groups <br> I have 4 groups of 3 . |  |




| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Multiplication is commutative | Create arrays using counters and cubes and Numicon. <br> Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer. | Use representations of arrays to show different calculations and explore commutativity. <br> $5 \times 2=10$ <br> $5 \times 2=10$ <br> 5 groups of 2 <br> 2 groups of 5 <br> 2, five times <br> 5, two times | Use an array to write multiplication sentences and reinforce repeated addition. $\begin{aligned} & 5+5+5=15 \\ & 3+3+3+3+3=15 \\ & 5 \times 3=15 \\ & 3 \times 5=15 \end{aligned}$ |





## Divisibility rules in 'families' $\mathbf{2 , 4} 4$ and 8

2 A number is divisible by 2 if the ones digit is even.
4 If halving a number gives an even value, then the number is divisible by 4 . and
For numbers with more than two digits: if the final two digits are divisible by 4 then the number is divisible by 4 .
8 If halving a number twice gives an even value, the number is divisible by 8 .

| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Multiplying 2-digit by 1 digit using partitioning (distributive law) | 4 rows of 10 4 rows of 3 <br> Show the links with arrays to illustrate the PV partitioning <br> Move onto base ten to move towards a more compact method. 4 rows of 13 <br> Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows | Children can represent their work with place value counters in a way that they understand. <br> They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below. | $\begin{gathered} 4 \times 10=40 \\ 4 \times 3=12 \\ 40+12=52 \end{gathered}$ |
| 2 digit x 1 digit using PV counters (no regrouping) | Chn can see array in the ones and the tens. There is a visual link to repeated addition. | Children practice, drawing their representations. $23 \times 3$ |  |




| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Understanding the commutative law. | 'Three groups of five are equal to fifteen.' 'Five, three times is equal to fifteen.' <br> B <br> - 'Five groups of three are equal to fifteen.' <br> "Three groups of five is equal to five groups of three." |  | $\begin{aligned} & 3 \times 5=15 \\ & 5 \times 3=15 \\ & 5 \times 3=3 \times 5=15 \\ & 15 \div 3=5 \\ & 15 \div 5=3 \end{aligned}$ |
| Understanding the distributive law |  <br> 3 <br>  |  | $4 \times 5=3 \times 5+5=20$ $4 \times 5=5 \times 5-5=20$ |


| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Multiply 3 digit numbers by 1 digit. (no exchange) | Use place value counters to show how we are <br> finding groups of a number. We are multiplying by 3 so we need 3 rows $123 \times 3=369$ <br> Add up each column, starting with the ones. | Children can represent their work with place value counters by drawing place value counters or Dienes. | 231 $3 \times 1$ ones is <br> three ones <br> $\times \quad 3$ <br> 693 $3 \times 3$ tens is <br> nine tens <br> $3 \times 2$ hundreds <br> is six hundreds |
| Multiply 3 digit numbers by 1 digit. (with exchange) |  <br> Regroup ten ones to make a new ten. |  |  |





| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Multiply decimals up to2 decimal places by a single digit |  |  | $\begin{array}{r} 2.38 \\ \times \quad 3 \\ \hline 714 \\ 12 \end{array}$ <br> First we lay out the calculation <br> Next, we write the decimal point in the answer (product). <br> Finally, we carry out the multiplication. <br> $3 \times 8$ hundredths is 24 hundredths <br> $3 \times 3$ tenths is 9 tenths, add 2 tenths we carried is 11 tenths <br> $3 \times 3$ ones is 6 ones, add 1 one we carried is 7 ones |
| Multiply up to 4 digit numbers by 2 digits. |  |  | $\begin{array}{llll}  & & x & \\ & 3 & 1 & 2 \\ \times & & 2 & 8 \\ \hline & & 4 & 9 \\ \hline \end{array}$ |






| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Division as sharing (partitive) | There are 20 conkers shared equally between 5 children. <br> Each child gets 4 conkers. | Children use pictures or shapes to share quantities. They may use bar modelling to show and support understanding. <br> Number lines are used to show skip counting (counting forwards) <br> and repeated subtraction (counting backwards). | $20 \div 5=4$ |
| Division as grouping (quotitive) | Use cubes, counters or real objects or to aid understanding. <br> There are 15 biscuits, there are 5 in each bag. How many bags? |  | 15 divided into groups of 5 is 3 $15 \div 5=3$ |





| Divisibility rules in 'families' $\mathbf{- 3 , 6}$ and $\mathbf{9}$ |  |
| :--- | :--- |
| $\mathbf{3}$ | For a number to be divisible by 3 , the sum <br> of the digits of the number must be divisible <br> by 3. |
| $\mathbf{6}$ | For a number to be divisible by 6, the number <br> must be divisible by both 2 and 3. |
| $\mathbf{9}$ | For a number to be divisible by 9 , the sum <br> of the digits of the number must be divisible <br> by 9. |

## Divisibility rules in 'families' - 5 and 10

5 A number is divisible by 5 if the ones digit is 5 or 0.
10 A number is divisible by 10 if the ones digit is 0 .



| Objective \& Strategy | Concrete | Pictorial | Abstract |
| :---: | :---: | :---: | :---: |
| Divide 2 \& 3 digit numbers by 1 digit <br> Short Division | $96 \div 3$ <br> Use place value counters to make groups of the divisor, starting with the largest value digit. <br> There are 3 groups of 3 tens. There are 2 groups of 3 ones. <br> There is 1 group of 3 tens. There is a ten left over. We exchange this for 10 ones. 12 ones divided by 3 is 4 . <br> There is 1 group of 4 hundreds. There are no groups of 4 tens and 3 tens left over. There are 8 groups of 4 ones after exchanging the left over tens. | Students use drawn diagrams with spots or circles to show their understanding. | Begin with divisions that divide equally with no remainder. $\begin{array}{r} 124 \\ 3 \longdiv { 3 7 2 } \end{array}$ <br> Move on to divisions with a remainder. Return to concrete if necessary. |


| Divisibility rules in numerical order |  |
| :--- | :--- |
| $\mathbf{2}$ | A number is divisible by 2 if the ones digit is even. |
| $\mathbf{3}$ | For a number to be divisible by 3, the sum of the <br> digits of the number must be divisible by 3. |
| $\mathbf{4}$ | If halving a number gives an even value, then the <br> number is divisible by 4. <br> and <br> For numbers with more than two digits: if the final <br> two digits are divisible by 4 then the number is <br> divisible by 4. |
| $\mathbf{5}$ | A number is divisible by 5 if the ones digit is <br> 5 or 0. |


| Divisibility rules in numerical order |  |
| :--- | :--- |
| $\mathbf{6}$ | For a number to be divisible by 6 , the number must <br> be divisible by both 2 and 3. |
| $\mathbf{8}$ | If halving a number twice gives an even value, the <br> number is divisible by 8. |
| $\mathbf{9}$ | For a number to be divisible by 9, the sum of the <br> digits of the number must be divisible by 9. |
| $\mathbf{1 0}$ | A number is divisible by 10 if the ones digit is 0. |





Using $\mathrm{x} \& \div$ by 10,100 etc and relating this to a short division method.


$$
\begin{array}{r}
0 \quad 2 \\
3 0 \longdiv { 6 \quad { } ^ { 6 } 0 }
\end{array}
$$

$\top \quad 0$
$3 0 \longdiv { 8 \quad 5 }$

T 0
2
$3 0 \longdiv { 8 \quad 5 }$
60

Subtract the 60 from

the 85 and this leaves

25. 

$3 0 \longdiv { 8 \quad 5 }$

$6 \quad 0$

25

30 goes into 85 twice, which is 60 .

85 divided by 30 is 2 with a remainder of

25


## Long Division-progressing to $\mathbf{4}$ or more digits



23 goes into 49 twice which is 46 . We subtract this from
49 to give a remainder of 3 .


We combine the 3 left over with the next digit to give 34.23 goes into 34 once with 11 remaining.

| TH | H | T | O |
| ---: | :---: | :---: | :---: |
|  | 2 | 1 | 5 |
| 4 | 9 | 4 | 5 |
| 4 | 6 |  |  |
|  | 3 | 4 |  |
|  | $\frac{2}{2}$ | 3 |  |
|  | 1 | 1 | 5 |
|  | 1 | 1 | 5 |
|  |  | 0 |  |

We combine the 11 with the
next digit to make 115. 23
goes into 1155 times with
no remainder.

## Long Division-procedural summary (remainder in the tens)

| 1. Divide. | 2. Multiply \& subtract. | 3. Drop down the next digit. |
| :---: | :---: | :---: |
| $\begin{array}{r} { }^{10} \\ 2 \longdiv { 2 } \\ \hline 2 \longdiv { 5 8 } \end{array}$ <br> Two goes into 5 two times, or 5 tens $+2=2$ whole tens -- but there is a remainder! | $\begin{gathered} t \circ \\ 2 \longdiv { 5 8 } \\ \frac{-4}{1} \end{gathered}$ <br> To find it, multiply $2 \times 2=4$, write that 4 under the five, and subtract to find the remainder of 1 ten. | $\begin{array}{r} t \circ \\ 29 \\ 2 \longdiv { 5 8 } \\ -41 \\ \hline 18 \end{array}$ <br> Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18 . |


| 1. Divide. | 2. Multiply \& subtract. | 3. Drop down the next digit. |
| :---: | :---: | :---: |
| $\begin{array}{r} t \circ \\ 29 \\ 2 \longdiv { 5 8 } \\ =-4 \\ 18 \end{array}$ <br> Divide 2 into 18. Place 9 into the quotient. | $\begin{array}{r} 1 \circ \\ 29 \\ 2 \longdiv { 5 8 } \\ -48 \\ \hline 18 \\ -18 \end{array}$ <br> Multiply $9 \times 2=18$, write that 18 under the 18 , and subtract. | $\begin{array}{r} t \circ \\ 29 \\ 2 \longdiv { 5 8 } \\ \frac{-4}{18} \\ -18 \\ \hline 0 \end{array}$ <br> The division is over since there are no more digits in the dividend. The quotient is 29 . |

## Long Division-procedural summary (remainder in any of the digits)

| 1. Divide. | 2. Multiply \& subtract. | 3. Drop down the next digit. |
| :---: | :---: | :---: |
| $\begin{aligned} & { }^{h t \circ} \\ & 2 \longdiv { 1 } \\ & 2 \longdiv { 2 7 8 } \end{aligned}$ <br> Two goes into 2 one time, or 2 hundreds $\div 2=1$ hundred. | $\begin{gathered} { }^{h t \circ} \\ 2 \longdiv { 2 7 8 } \\ \frac{-2}{0} \end{gathered}$ <br> Multiply $1 \times 2=2$, write that 2 under the two, and subtract to find the remainder of zero. | $\begin{gathered} h t o \\ 18 \\ 2 \longdiv { 2 7 8 } \\ -\frac{2}{0} \frac{1}{7} \end{gathered}$ <br> Next, drop down the 7 of the tens next to the zero. |
| Divide. | Multiply \& subtract. | Drop down the next digit. |
| $\begin{gathered} \begin{array}{c} h+0 \\ 13 \\ 2 \longdiv { 2 7 8 } \\ -2 \\ \hline 07 \end{array} \end{gathered}$ <br> Divide 2 into 7. Place 3 into the quotient. | $\begin{gathered} h+0 \\ 13 \\ 2 \longdiv { 2 7 8 } \\ -\frac{2}{07} \\ -\quad 6 \\ \hline 1 \end{gathered}$ <br> Multiply $3 \times 2=6$, write that 6 under the 7 , and subtract to find the remainder of 1 ten. | $\begin{gathered} h t o \\ 13 \\ 2 \longdiv { 2 7 8 } \\ -\frac{2}{07} \\ -\quad 6 \\ \hline 18 \end{gathered}$ <br> Next, drop down the 8 of the ones next to the 1 leftover ten. |
| 1. Divide. | 2. Multiply \& subtract. | 3. Drop down the next digit. |
| $\begin{gathered} h 10 \\ 139 \\ 2 \longdiv { 2 7 8 } \\ -27 \\ -07 \\ -\quad 6 \\ \hline 18 \end{gathered}$ <br> Divide 2 into 18. Place 9 into the quotient. | $\begin{aligned} & h+0 \\ & 139 \\ & 2 \longdiv { 2 7 8 } \\ & -2 \\ & \hline 07 \\ & -\quad 6 \\ & \hline \quad 18 \\ & -18 \\ & \hline \end{aligned}$ <br> Multiply $9 \times 2=18$, write that 18 under the 18 , and subtract to find the remainder of zero. | $\begin{aligned} & h+0 \\ & 2 \longdiv { 1 3 9 } \\ & 278 \\ & -27 \\ & -\quad 6 \\ & -18 \\ & -18 \end{aligned}$ <br> There are no more digits to drop down. The quotient is 139 . |

